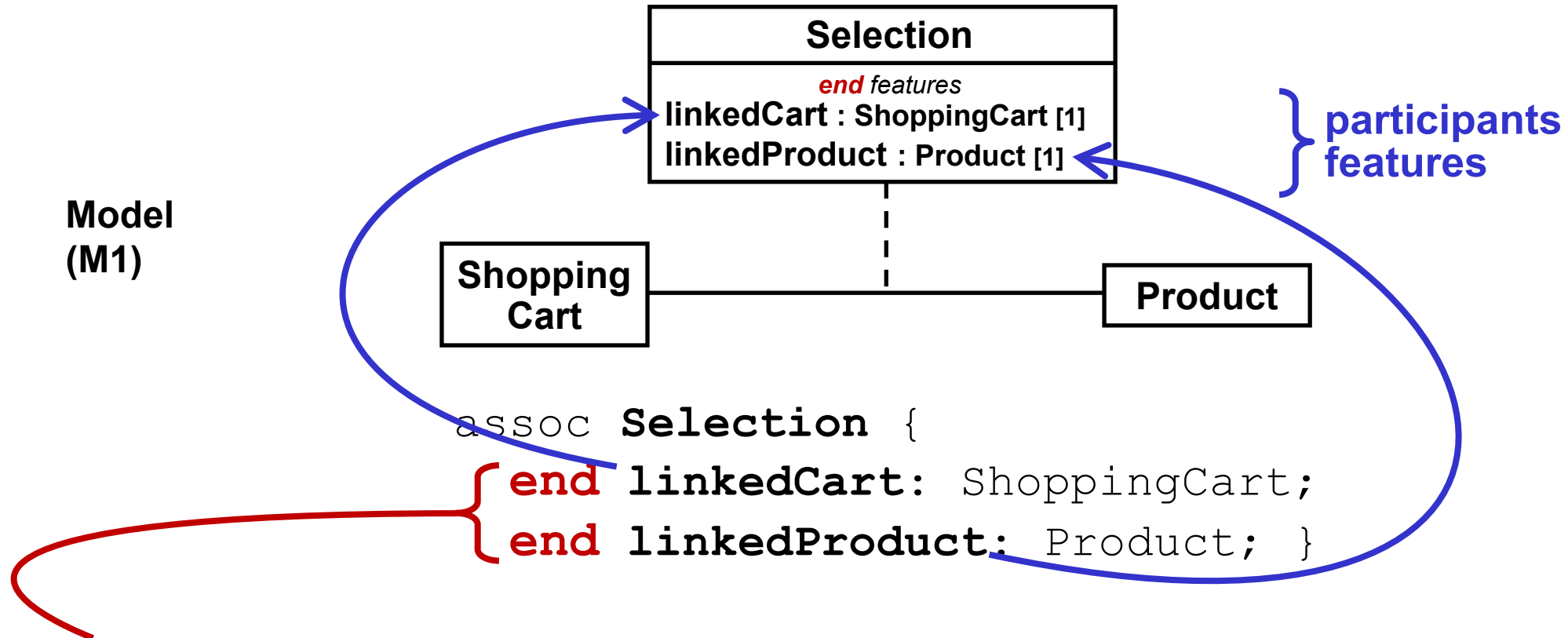


# Overview

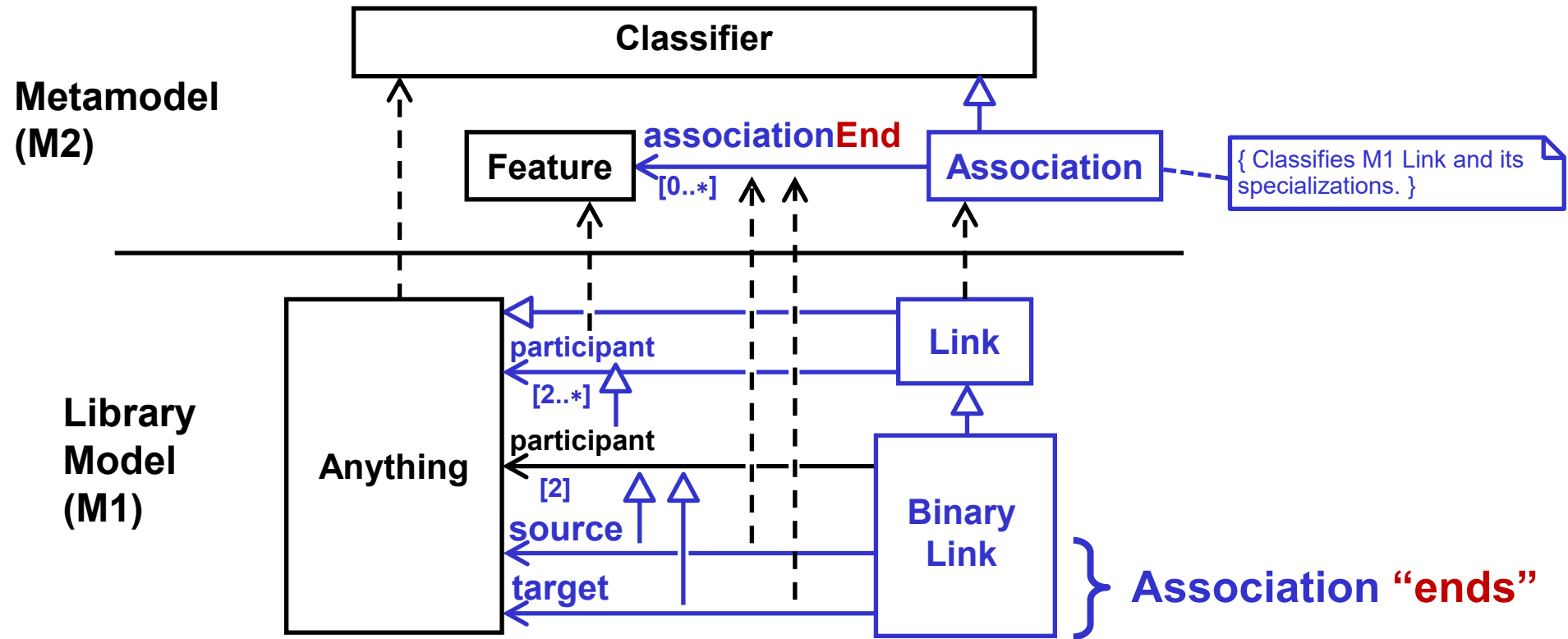
- Associations
- Debt (SysML1 & SST)
  - Paid (SST February)
  - **Unresolved (still paying interest)**
- Proposals
- Summary

# Assoc “Ends” (textual syntax)



- KerML “end” features are actually participant features.
  - Values are the things being linked, exactly one each.
  - Better term? Needs to be short, not an abbreviation.

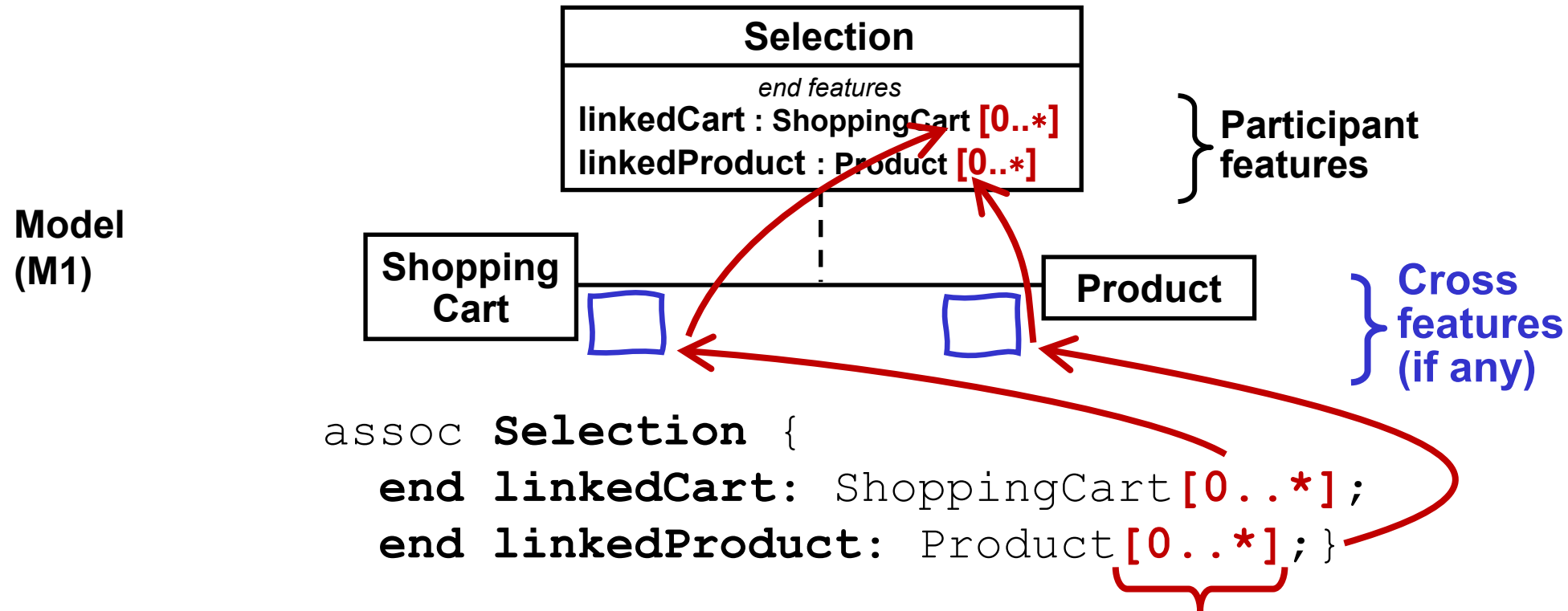
# Assoc “Ends” (abstract syntax)



- Same term in the metamodel.

# Assoc Textual Syntax (multiplicity)

KERML-26



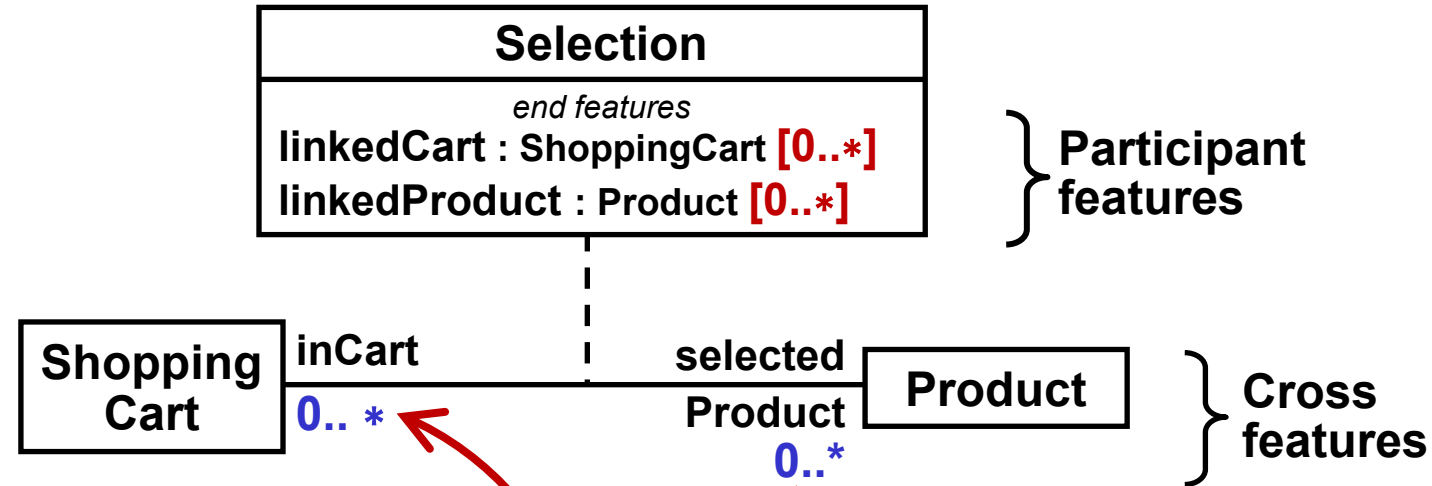
- “End” multiplicity is about **cross features** ...,
- ... which **might not exist**.
  - **Useful** for one-way and non-navigable associations.
- **Looks like participant** multiplicity (if you know “end”).

Same for  
ordering and  
uniqueness

# Assoc Textual Syntax (multiplicity)

KERML-36

Model  
(M1)



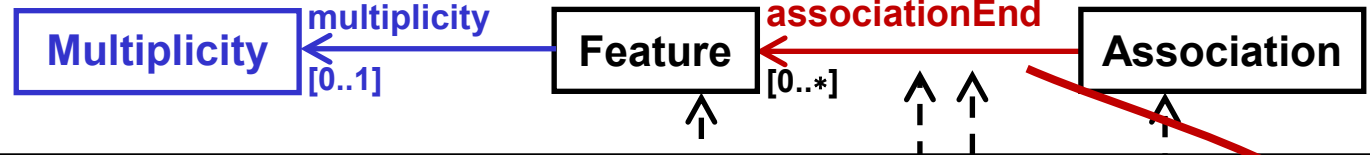
```
assoc Selection {  
  end linkedCart: ShoppingCart [0..*] subsets linkedProduct.inCart;  
  end linkedProduct: Product [0..*] subsets linkedCart.selectedProduct;  
}
```

- “End” multiplicity **redundant** and possibly **conflicting**
  - between “end” and cross features.
- In textual **and** abstract syntax.

Same for  
ordering and  
uniqueness

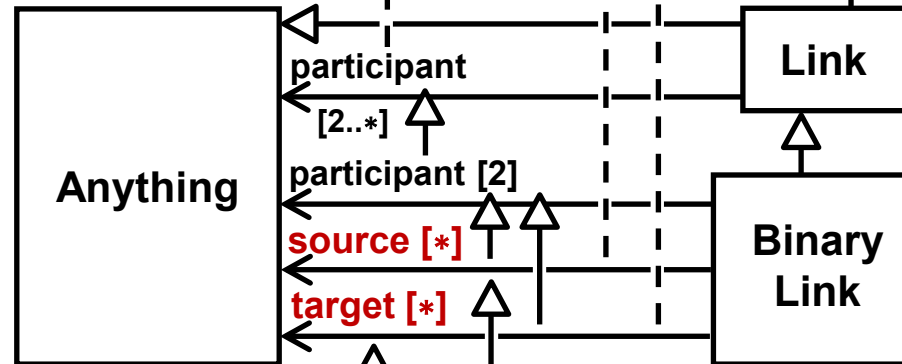
# Assoc Abstract Syntax (multiplicity)

Metamodel  
(M2)



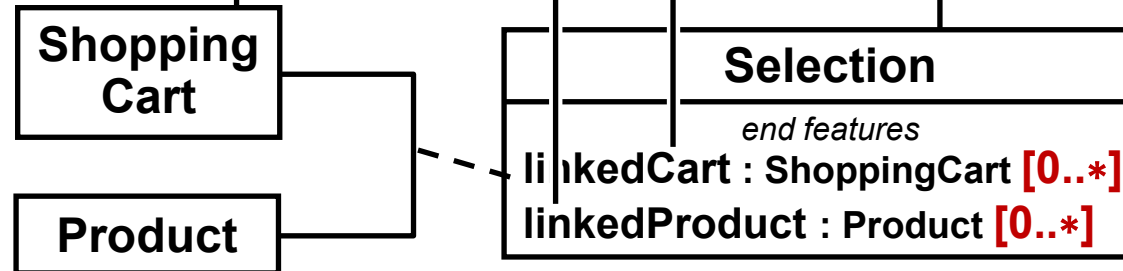
[KERML-37](#)  
[KERML-35](#)  
[KERML-55](#)  
[KERML-38](#)

Library  
(M1)



**Changes meaning of multiplicity to be about cross features**

Model  
(M1)



System  
(M1)



- **“End” changes feature multiplicity semantics** ..
  - ... to be about cross features.
  - Number of participant feature values **not restricted**.

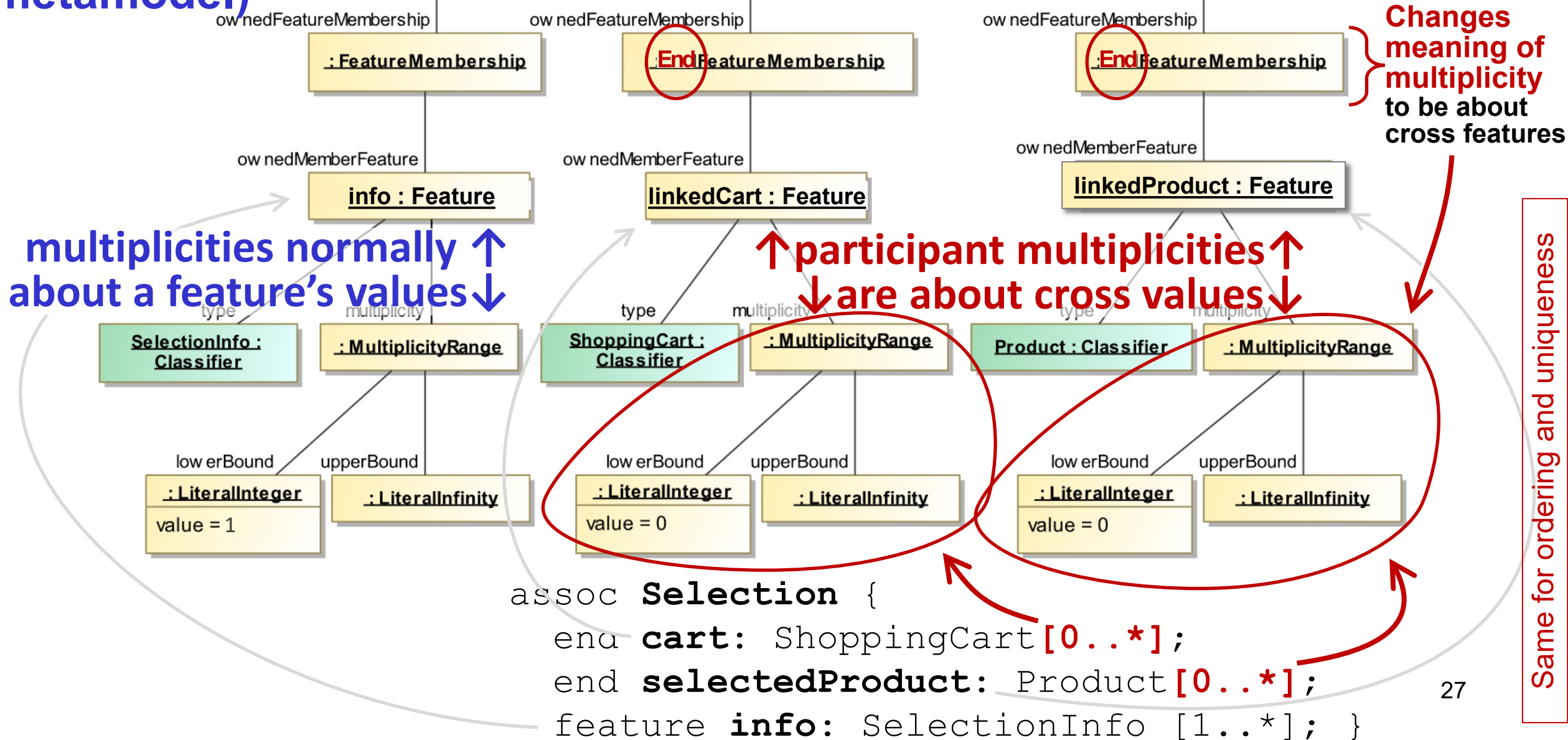
**Same for ordering and uniqueness**

# KerML Associations

(instances of metamodel)

[KERML-37](#) [KERML-35](#)

[KERML-38](#) [KERML-55](#)



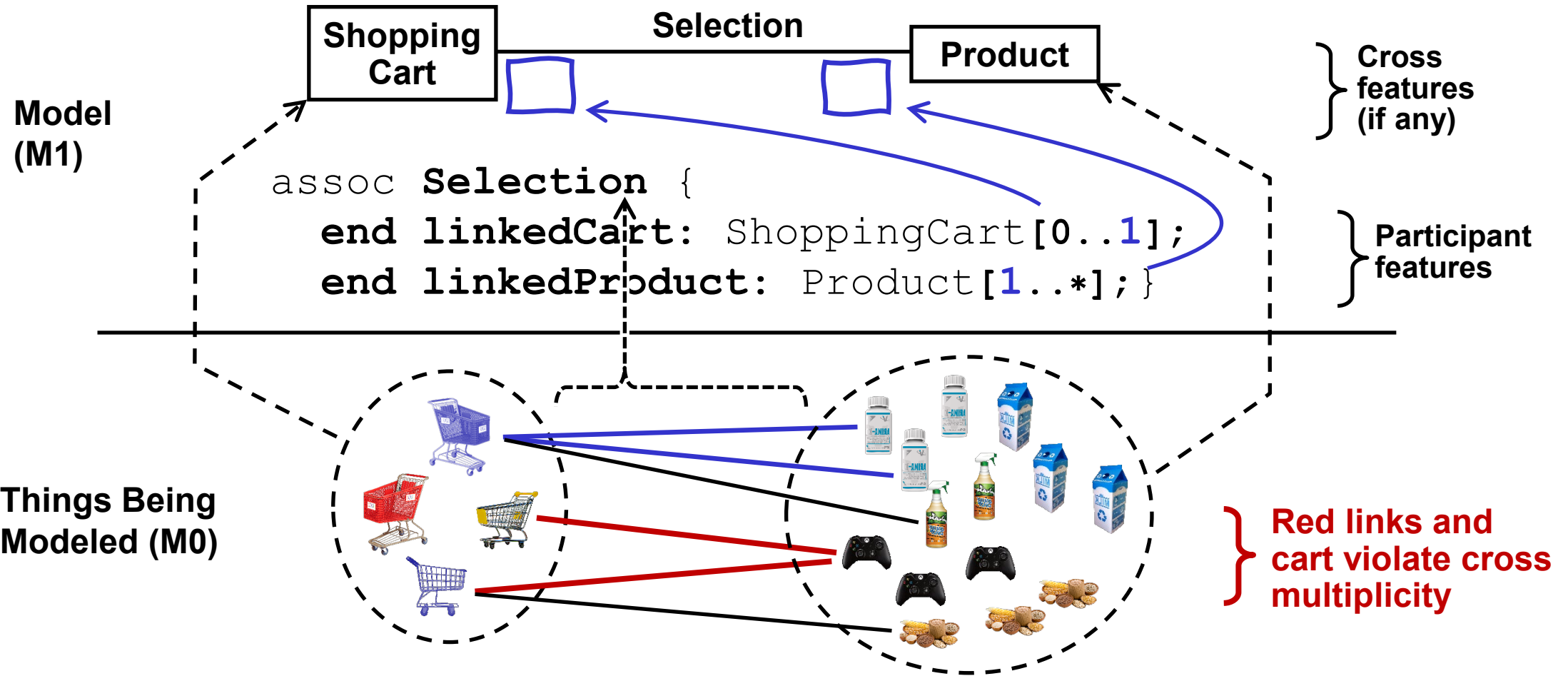
Changes meaning of multiplicity to be about cross features

multiplicities normally ↑ about a feature's values ↓

↑ participant multiplicities ↑ are about cross values ↓

Same for ordering and uniqueness

# Assoc Semantics (cross multiplicity)



- **Every cart and product must satisfy cross multiplicity.**  
– via Selection links.



# Assoc Semantics (cross multiplicity)

KERML-40

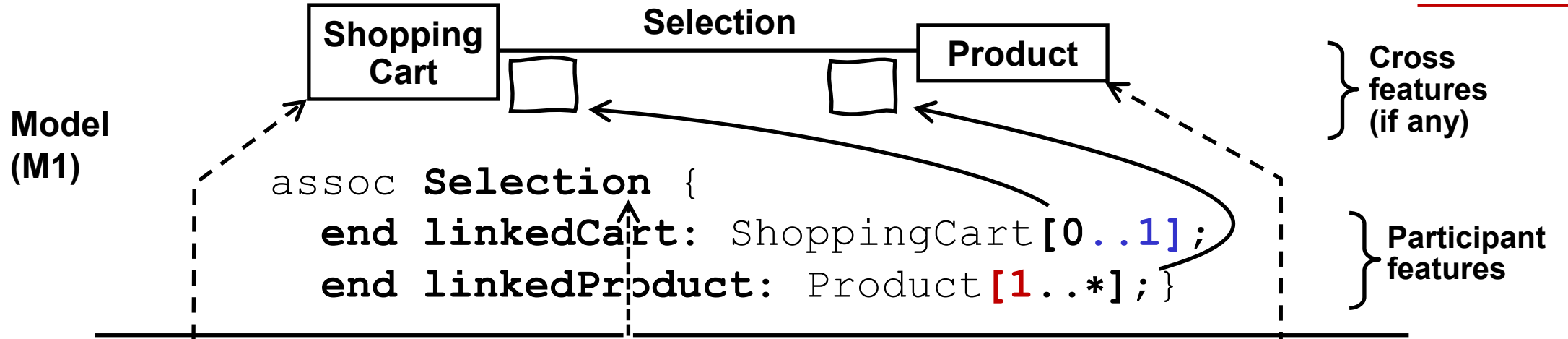
- **Informal** text currently.
- **Applies only to instances of association (links),**
  - **rather than instances of the associated classifiers.**

[7.4.5] if an association end has a multiplicity specified other than 1..1, then this is interpreted as follows: *For each association end, the multiplicity, ordering and uniqueness constraints specified for that end **apply to each set of instance of the association that have the same (single) values for each of the other ends.*** For a binary association, this corresponds to the multiplicity resulting from "navigating" across the association given a value at one end of the association to the other end of the association.

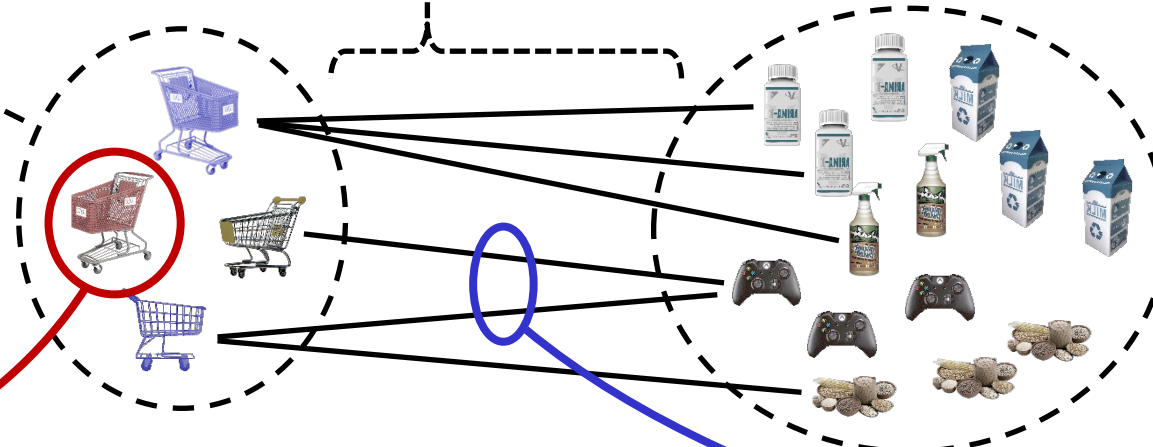
[8.4.4.5.1] If an associationEnd has a declared multiplicity other than 1..1, then this shall be interpreted as follows: For an Association with  $N$  associationEnds, consider the  $i$ -th associationEnd  $e_i$ . *The multiplicity, ordering and uniqueness constraints specified for  $e_i$  **apply to each set of instances of the Association that have the same (singleton) values for each of the  $N-1$  associationEnds other than  $e_i$ .***

# Assoc Semantics (cross multiplicity)

KERML-40



Things Being Modeled (M0)



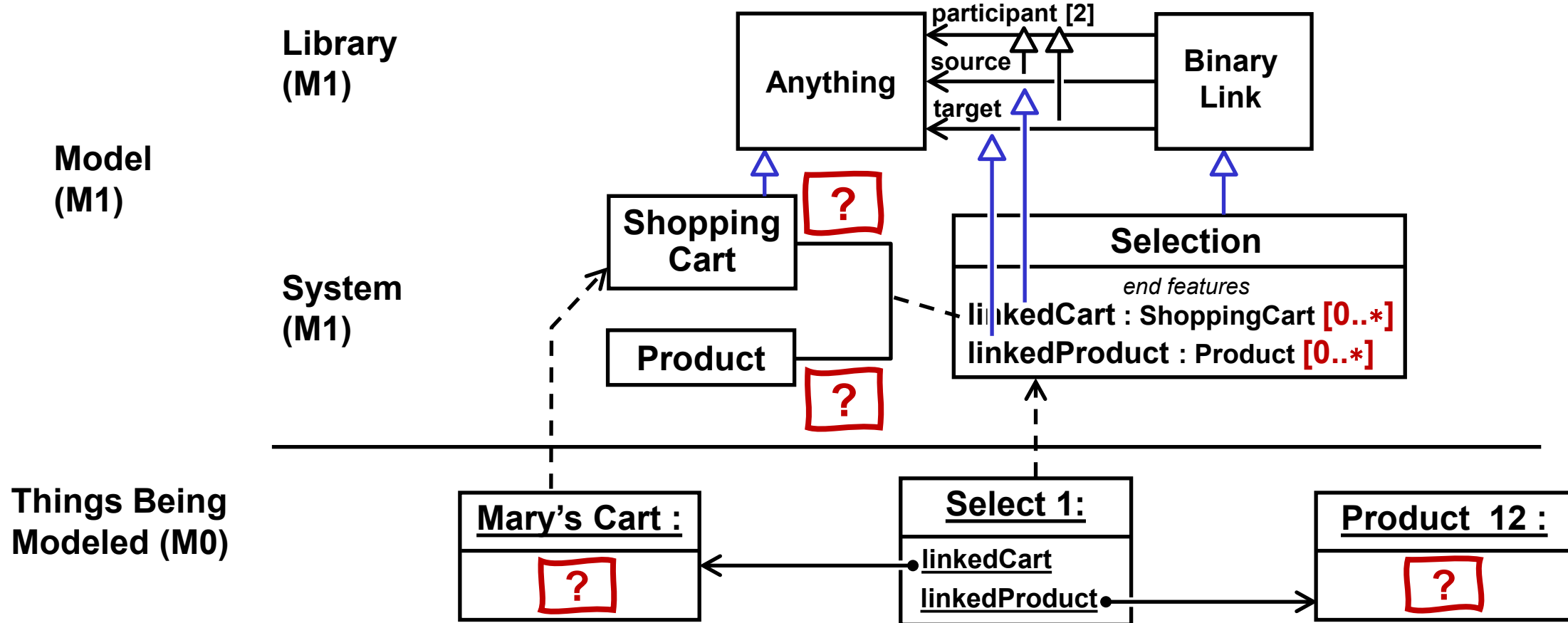
**Misses this violation**

**Catches this violation**

**Semantics only applies to association instances**

# Assoc, Identifying Cross Features

KERML-41



- Nothing in the textual or abstract syntax for them.
  - Cross-subsetting chain pattern is **modeler option**.
  - **API access** can't depend on it, eg, for automated analysis.

# Association Debt Summary

## 1. Misleading textual syntax

- Term: “end” for participant rather than cross features [KERML-34](#)
- Cross feature multiplicity looks like participant’s. [KERML-26](#)

## 2. Two meanings for feature multiplicity

- Requires special casing in modeling/analysis tools. [KERML-37](#)  
[KERML-55](#)  
[KERML-38](#)
- Redundant cross feature multiplicity [KERML-36](#)

## 3. Incomplete semantics

- Number of participant values not restricted (should be [1]). [KERML-35](#)
- Cross multiplicity semantics is informal and incomplete.

## 4. Cross features not identified [KERML-41](#)

- Subsetting pattern is non-standard (tool builders and modelers cannot depend on it). [KERML-40](#)

# Overview

- Associations
- Debt (SysML1 & SST)
  - Paid (SST February)
  - Unresolved (still paying interest)
- **Proposals**
- Summary

# Assoc Participant Textual Syntax (Proposal)

[KERML-34](#)

[KERML-26](#)

Model  
(M1)



} Participant features

System  
(M1)



} Cross features (if any)

```
assoc Selection {  
  linkEnd [0..*] linkedCart: ShoppingCart;  
  linkEnd [0..*] linkedProduct: Product;}  
  
```

Same for ordering and uniqueness

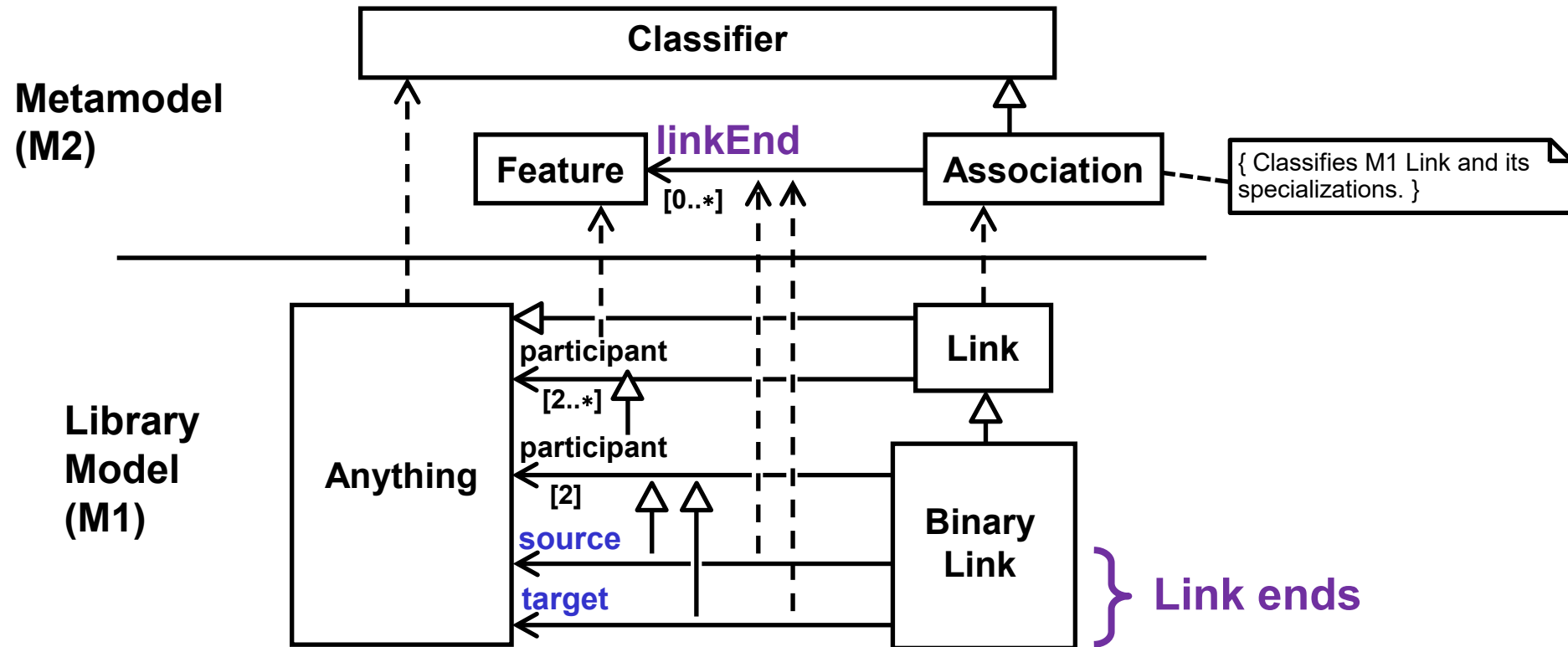
Library  
(M1)

```
  > assoc BinaryLink {  
    linkEnd source: Anything [1] subsets participant;  
    linkEnd target: Anything [1] subsets participant;}  
  
```

- **Keyword and cross multiplicity position change.**
  - Leaves (textual) room for **participant multiplicity** in library.

# Assoc Participant Abstract Syntax (Proposal)

KERML-34



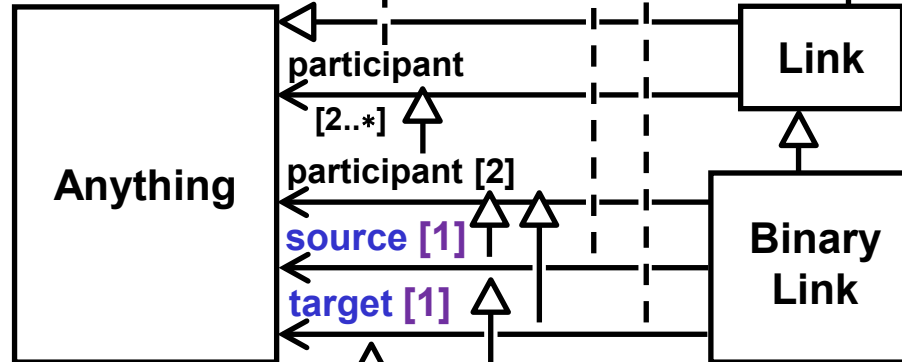
- **Same term in the metamodel.**

# Assoc Participant Semantics (Proposal)

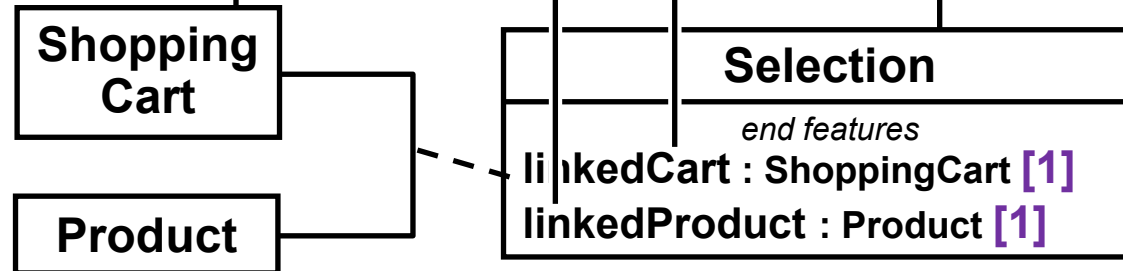
Metamodel  
(M2)



Library  
(M1)



Model  
(M1)



System  
(M1)



[KERML-37](#)

[KERML-35](#)

[KERML-55](#)

[KERML-38](#)

No change to meaning of multiplicity

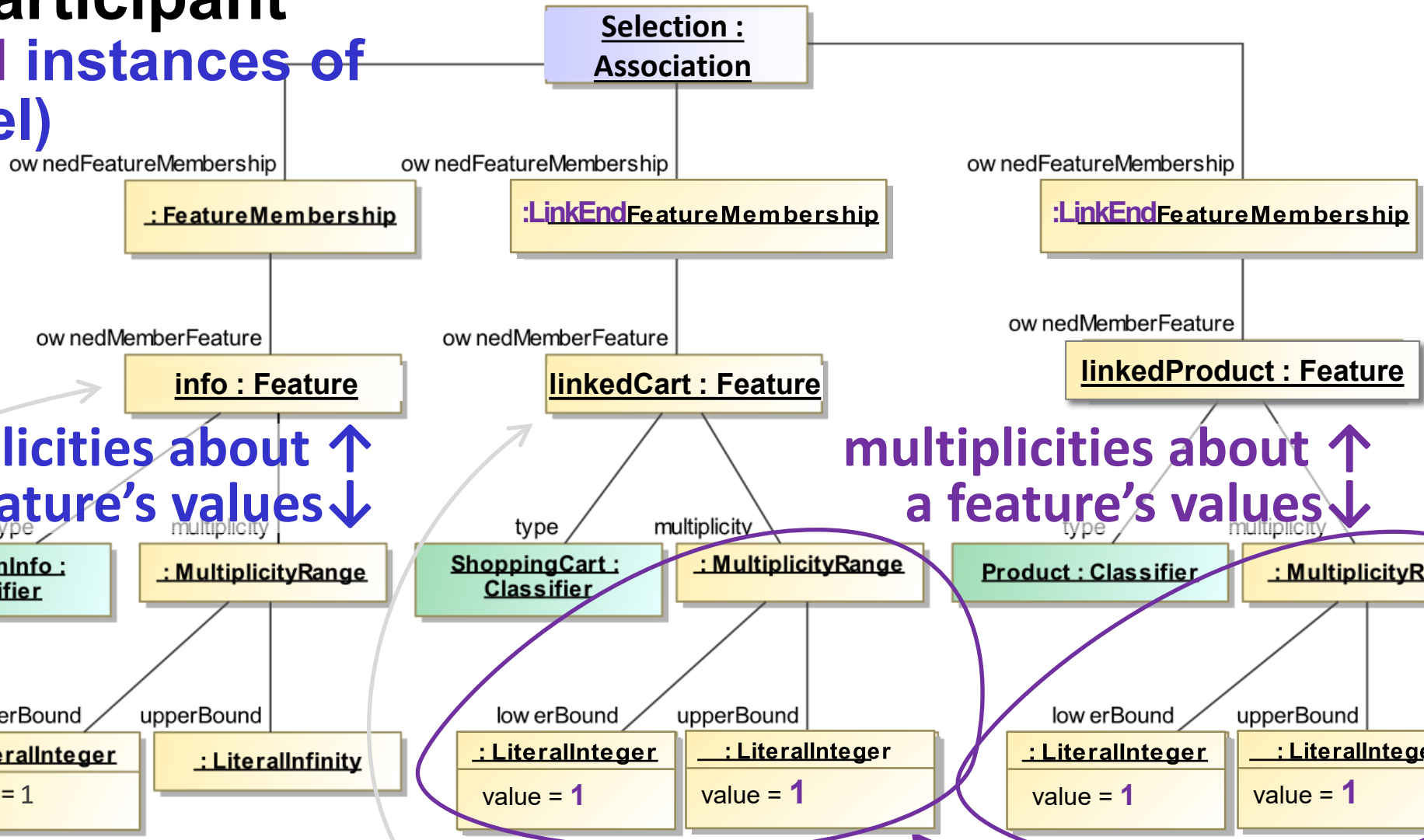
Same for ordering and uniqueness

- No change in feature multiplicity semantics ...
  - ... to be about cross features.
  - Number of participant feature values restricted to 1.



# Assoc Participant (proposed instances of metamodel)

[KERML-37](#)  
[KERML-35](#)  
[KERML-55](#)  
[KERML-38](#)



No change in meaning of multiplicity

multiplicities about ↑  
a feature's values ↓

multiplicities about ↑  
a feature's values ↓

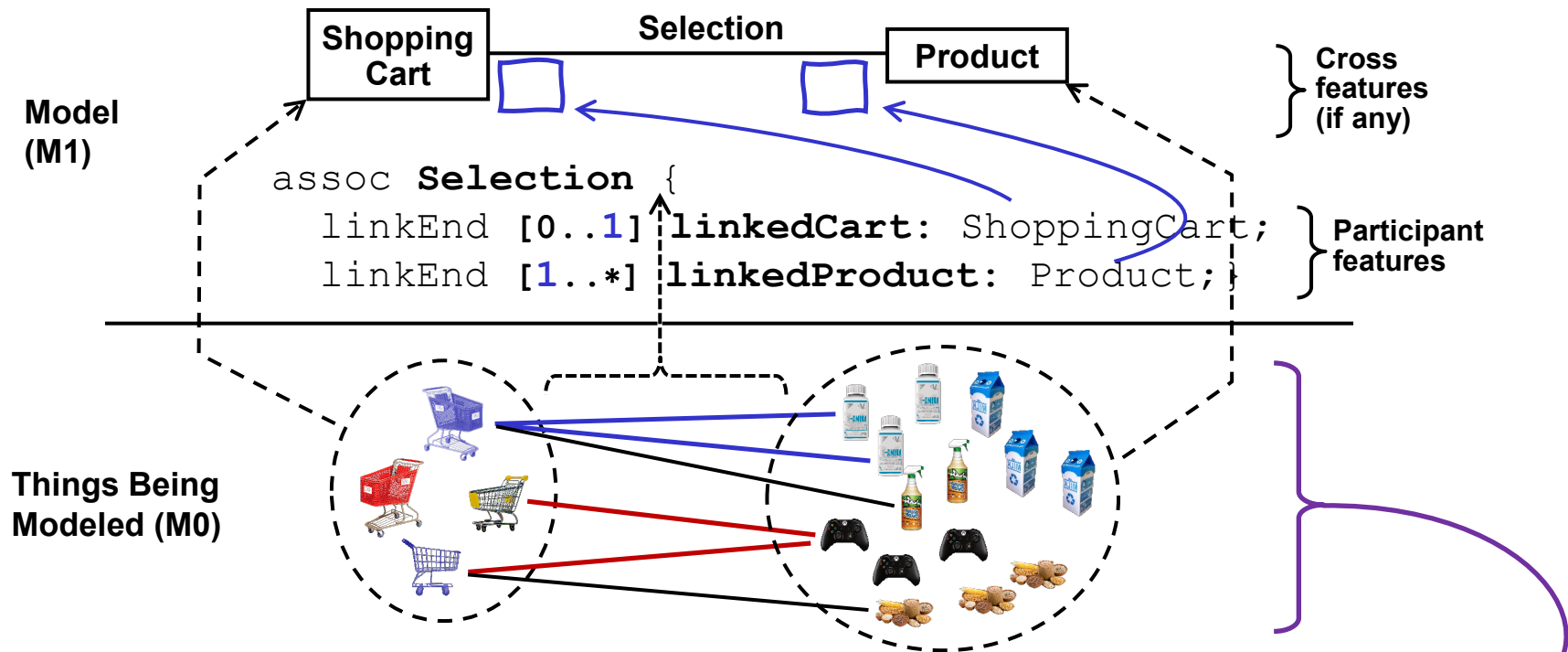
```

assoc Selection {
end cart: ShoppingCart [1];
end selectedProduct: Product [1];
feature info: SelectionInfo [1..*]; }
  
```

Same for ordering and uniqueness

# Assoc Cross Feature Semantics (How?)

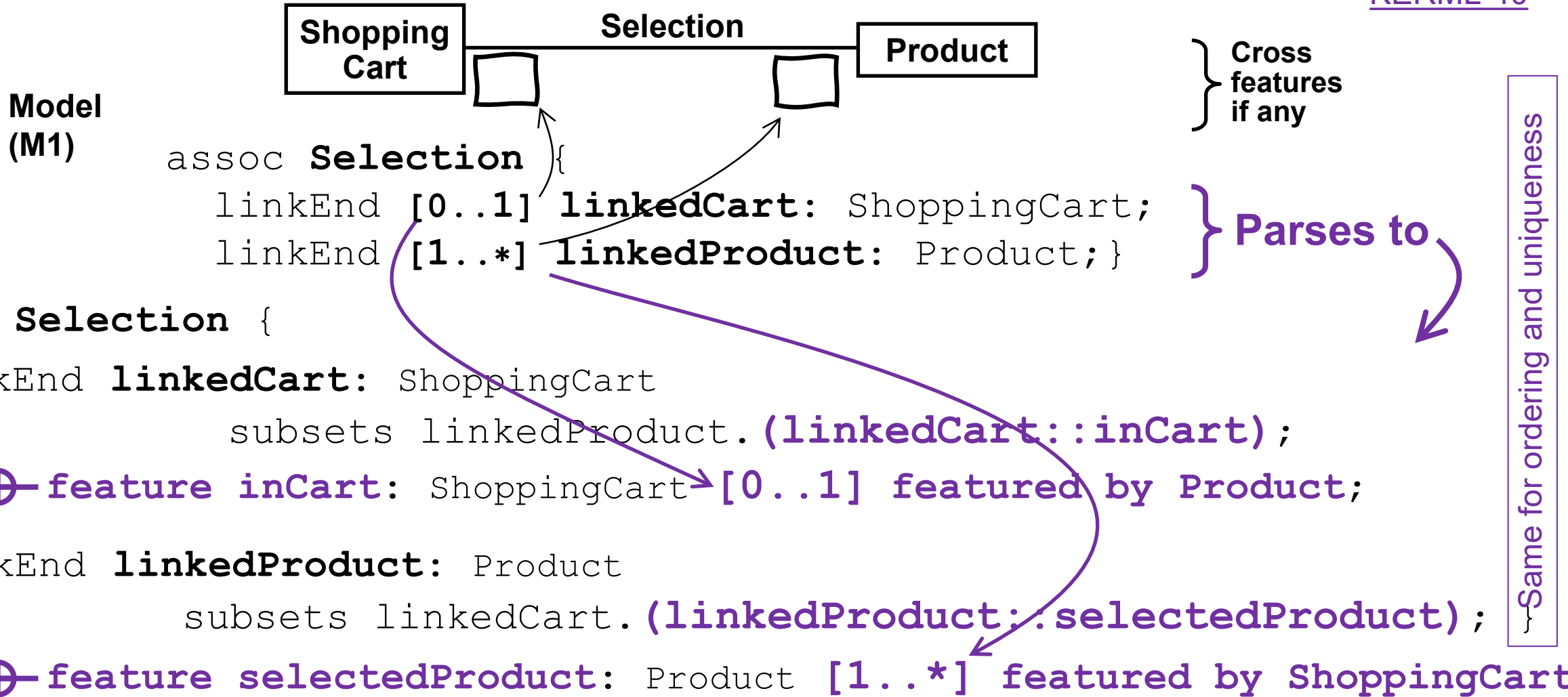
KERML-40



- How constrain all instances collectively?
  - Of association and its associated classifiers
- Usually done in math semantics
  - Trying to use math only in Core.

# Cross Feature Modeled Semantics (Proposal)

KERML-40



- Cross features in participant namespace.

# Cross Feature ~~Redundancy~~ (Proposal)

KERML-36

Model (M1)



} Cross features

```

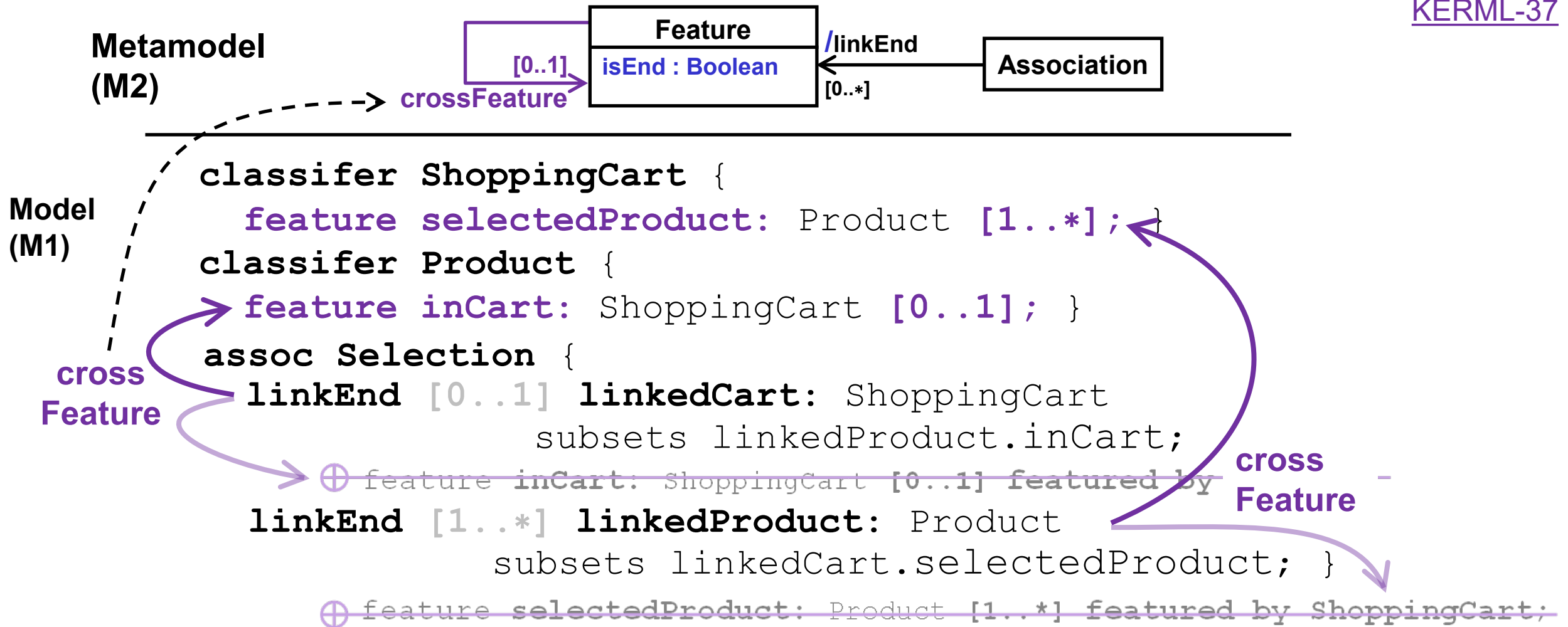
classifier ShoppingCart {
    feature selectedProduct: Product [1..*];
}
classifier Product {
    feature inCart: ShoppingCart [0..1];
}
assoc Selection {
    linkEnd [0..1] linkedCart: ShoppingCart
        subsets linkedProduct.inCart;
    ⊕ feature inCart: ShoppingCart [0..1] featured by Product;
    linkEnd [1..*] linkedProduct: Product
        subsets linkedCart.selectedProduct;
    ⊕ feature selectedProduct: Product [1..*] featured by ShoppingCart;
}
    
```

Same for ordering and uniqueness

- **Move cross features to associated classifiers**
  - As UML/SysML tools currently do with “association-owned ends”.

# Cross Feature Abstract Syntax (Proposal)

KERML-37



- Participant (link end) features **identify** cross features
  - As UML/SysML associations currently do with assoc ends.

# Participant, Identify Cross Subsets (Proposal)

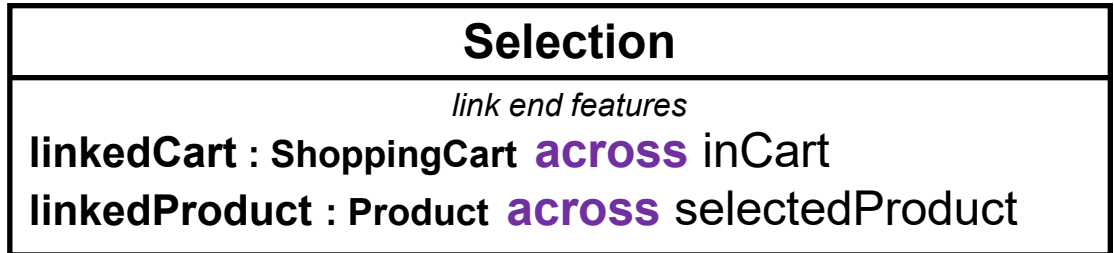
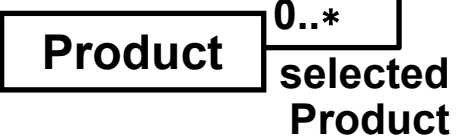
KERML-41

Metamodel  
(M2)



- For binary associations:
- source must be link end feature that identifies a cross feature
  - target must chain through other link end feature then cross feature

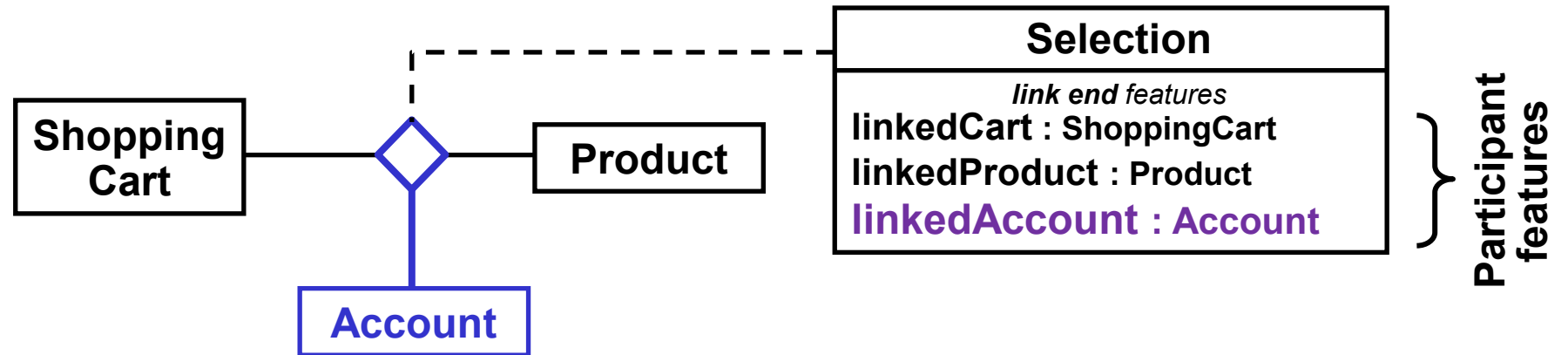
Model  
(M1)



```

assoc Selection {
  linkEnd [0..*] linkedCart: ShoppingCart across inCart;
  linkEnd [0..1] linkedProduct: Product across selectedProduct;
}
  
```

# “N”-aries ( > 2 participants)

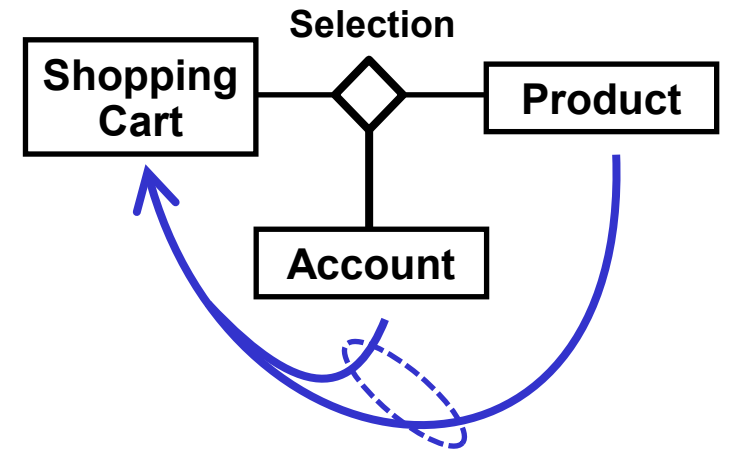
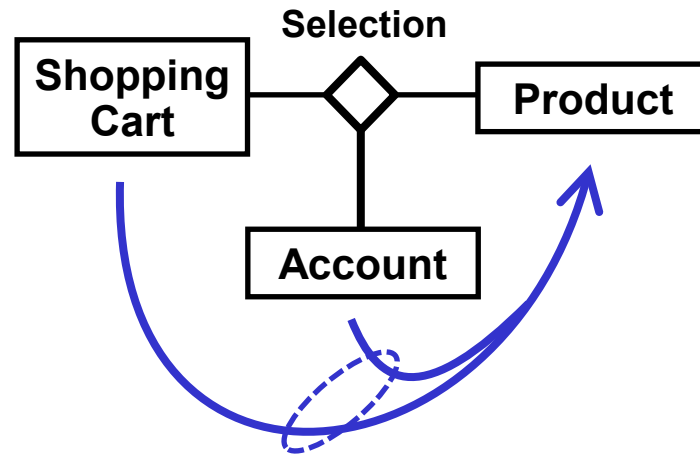
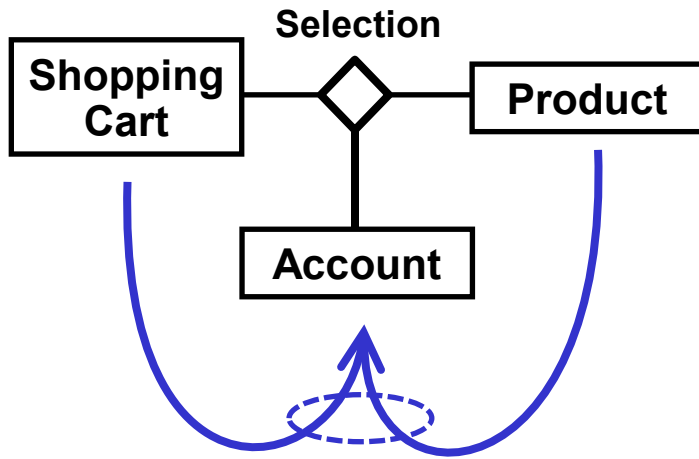


```
assoc Selection {  
  linkEnd linkedCart: ShoppingCart [1] subsets participant;  
  linkEnd linkedProduct: Product [1] subsets participant;  
  linkEnd linkedAccount: Account [1] subsets participant;  
  feature redefines participant: Anything [3] }  
assoc Link {  
  feature participant: Anything [2..*]; }  
  
```

Blue arrows indicate that the `linkedAccount` feature in the `Selection` class redefines the `participant` feature in the `Link` class. The `participant` feature in the `Link` class is also shown to be a specialization of the `participant` feature in the `Selection` class.

- **Specialize Link & participant directly.**

# “N”-aries ( > 2 participants) “Navigation”



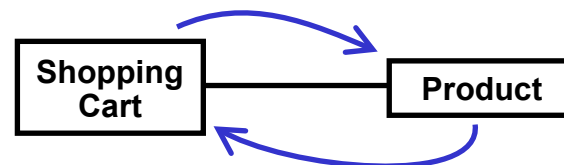
a shopping cart + a product → account

a shopping cart + an account → product(s)

a product + an account → shopping cart

- Association end (cross) multiplicity, ordering, and uniqueness apply to “navigation” from n-1 things.

– Generalized from n=2.





# “N”-ary Cross Features (Proposal)

KERML-40

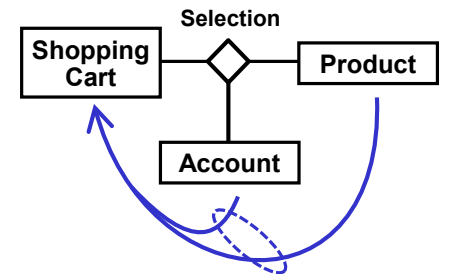
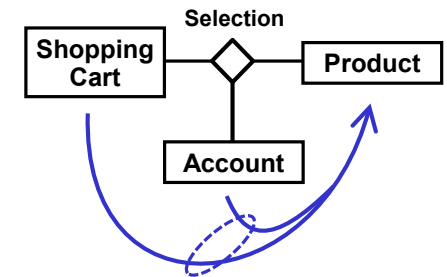
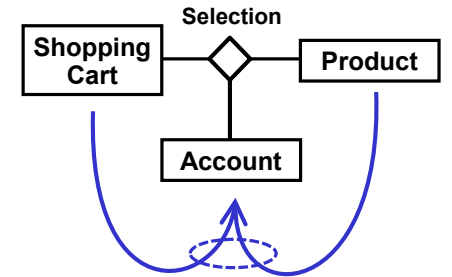
- Domains are sequences of “n-1” data types.

```
datatype CartProductPair specializes OrderedPair {  
  redefines element1: Cart;  
  redefines element2: Product; }
```

```
datatype CartAccountPair specializes OrderedPair {  
  redefines element1: Cart;  
  redefines element2: Account; }
```

```
datatype ProductAccountPair specializes OrderedPair {  
  redefines element1: Product;  
  redefines element2: Account; }
```

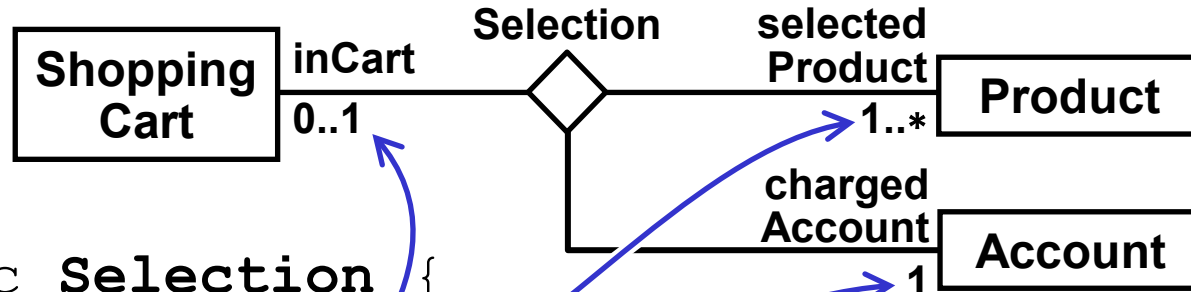
```
datatype OrderedPair specializes OrderedCollection {  
  feature redefines elements [2];  
  feature element1 [1] = elements#(1); feature element2 [1] = elements#(2); }
```



# N-ary Assoc Modeled Semantics (Proposal)

KERML-40

Model (M1)



```

assoc Selection {
  linkEnd [0..1] linkedCart: ShoppingCart;
  linkEnd [1..*] linkedProduct: Product;
  linkEnd [1] linkedAccount: Account; }
  
```

} Parses to

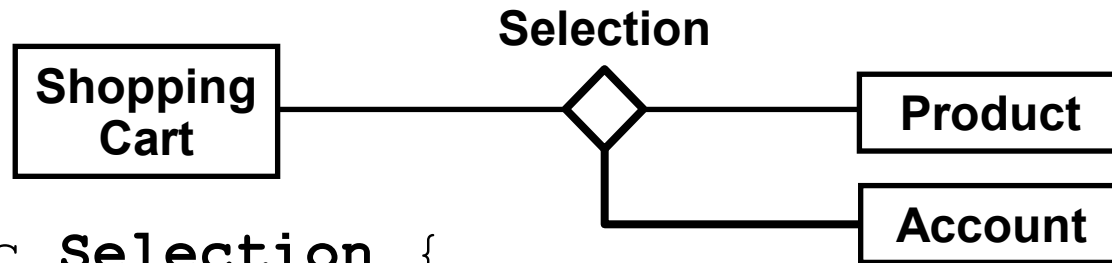
```

assoc Selection {
  linkEnd linkedCart: ShoppingCart;
  ⊕ feature inCart: ShoppingCart [0..1] featured by ProductAcntPair;
  linkEnd linkedProduct: Product;
  ⊕ feature selectedProduct: Product [1..*] featured by CartAcntPair;
  linkEnd linkedAccount: Account;
  ⊕ feature chargedAccount: Account [1] featured by CartProductPair;
}
  
```

Same for ordering and uniqueness

# N-ary Assoc Modeled Semantics (Proposal)

KERML-40



Model  
(M1)

```
assoc Selection {  
  linkEnd [0..1] linkedCart: ShoppingCart;  
  linkEnd [1..*] linkedProduct: Product;  
  linkEnd [1] linkedBuyer: Account; }
```

} Parses to

```
assoc Selection {  
  linkEnd linkedCart: ShoppingCart  
    subsets (linkedProduct, linkedAccount). (linkedCart::inCart);  
    ⊕-feature inCart: ShoppingCart [0..1] featured by ProductAcctPair;  
  linkEnd linkedProduct: Product  
    subsets (linkedCart, linkedAccount). (linkedProduct::selectedProduct); }  
    ⊕-feature selectedProduct: Product [1..*] featured by CartAcctPair;  
  linkEnd linkedAccount: Account  
    subsets (linkedCart, linkedProduct). (linkedBuyer::productBuyer); }  
    ⊕-feature productBuyer: Account [1] featured by CartProductPair;
```

Same for ordering and uniqueness

# N-ary, Identify Cross Subsets (Proposal)

KERML-41

Metamodel  
(M2)

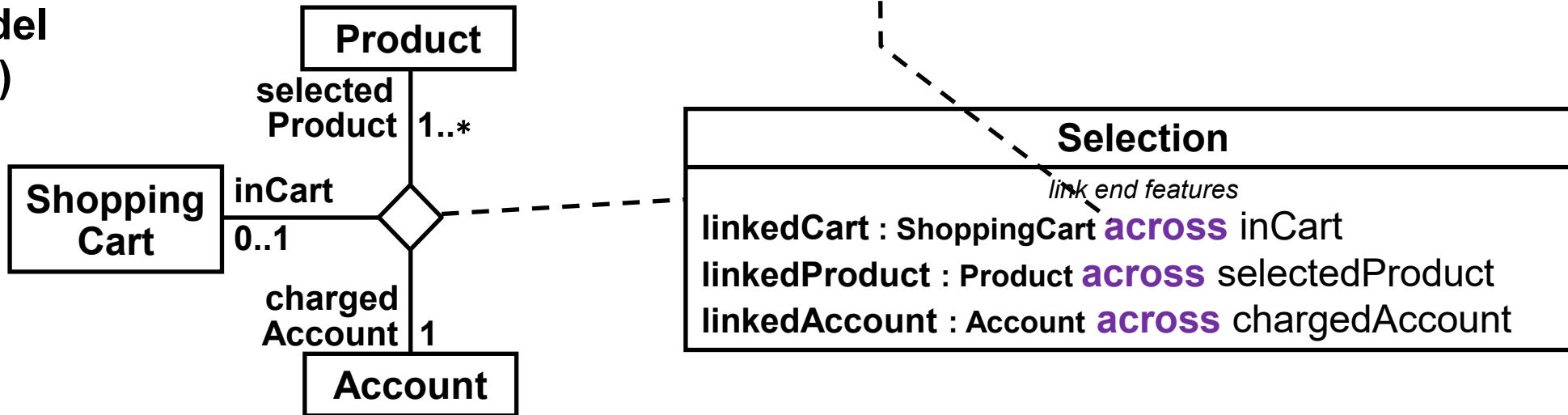
Subsetting

Crossing

For *n*-ary associations:

- source must be link end feature that identifies a cross feature
- target must chain through **sequence of other “n-1” link end values, then cross feature**

Model  
(M1)



```

assoc Selection {
  linkEnd [0..1] linkedCart: ShoppingCart across inCart;
  linkEnd [1..*] linkedProduct: Product across selectedProduct;
  linkEnd [1] linkedAccount: Account across chargedAccount;
}
    
```